There are multiple options for most third register trills and different fingerings work better on certain flutes and for certain people. Note the piccolos are often even fussier than flutes and the same fingerings that work on flute might not work on piccolo.